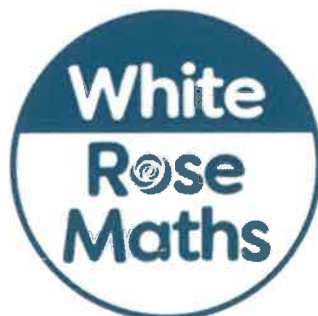


# Penclawdd Primary School

## Maths Calculation Strategies



## Mathematics and Numeracy

At Penclawdd Primary School, we use the White Rose Maths scheme for the teaching of Maths from Reception to Year 6, which follows the mastery approach to learning. At the heart of White Rose Maths is the belief that all children can achieve.

White Rose Maths focuses on helping all children to build a deep understanding of maths concepts and confidence in maths.

For each year group the curriculum strands are broken down into small steps that build on prior knowledge to help children develop a deep and robust understanding of the concept before moving on.

Within this booklet, you will find the calculation strategies taught and used by your child in school.

Further information can be found at [www.whiteroseeducation.com](http://www.whiteroseeducation.com)

# Progression of skills - Addition

Year group	Skill
Nursery	<ul style="list-style-type: none"><li>• Subitise to 3</li><li>• Count how many</li><li>• Make numbers to 5</li><li>• Add 1 more (through songs and rhymes)</li></ul>
Reception	<ul style="list-style-type: none"><li>• Conceptually subitise to 5</li><li>• 1 more</li><li>• Notice the composition of numbers within 10</li><li>• Combine 2 groups</li><li>• Add more</li></ul>
Year 1	<ul style="list-style-type: none"><li>• Add together</li><li>• Add more</li><li>• Bonds within 10</li><li>• Related facts within 20</li><li>• Missing numbers</li></ul>

# Progression of skills - Addition

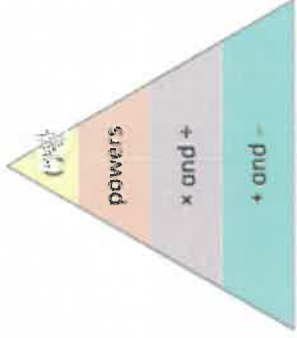



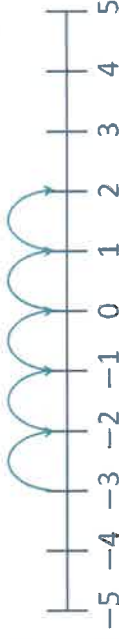
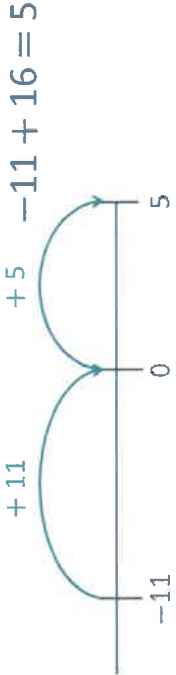
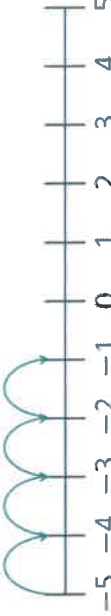
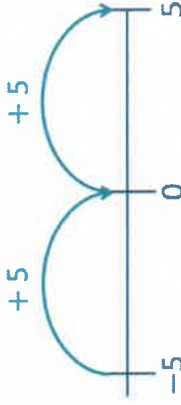
Year group	Skill
Year 2	<ul style="list-style-type: none"><li>• Add 1s to any number (related facts)</li><li>• Add three 1-digit numbers</li><li>• Add across a 10</li><li>• Add multiples of 10</li><li>• Add 10s to any number</li><li>• Add two 2-digit numbers (not across a ten)</li><li>• Add two 2-digit numbers (across a ten)</li><li>• Missing numbers</li></ul>
Year 3	<ul style="list-style-type: none"><li>• Add 1s, 10s and 100s to a 3-digit number</li><li>• Add two numbers (no exchange)</li><li>• Add two numbers across a 10 or 100</li><li>• Complements to 100</li><li>• Add fractions with the same denominator within 1 whole</li><li>• Calculate the duration of events</li></ul>

# Progression of skills - Addition


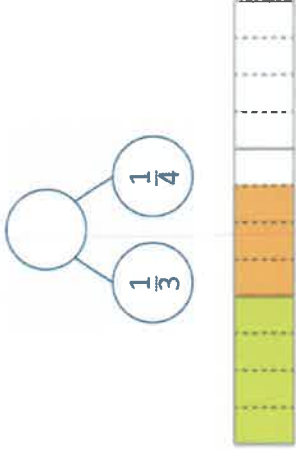
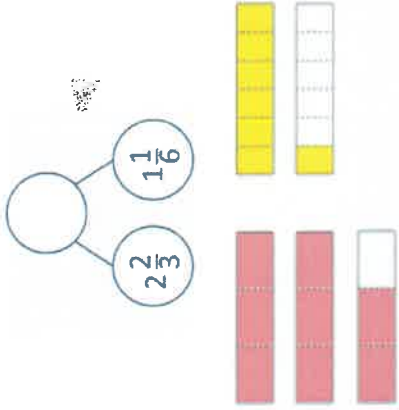
Year group	Skill
Year 4	<ul style="list-style-type: none"><li>• Add 1s, 10s and 100s to a 4-digit number</li><li>• Add up to two 4-digit numbers</li><li>• Add decimal numbers in the context of money</li><li>• Add fractions and mixed numbers with the same denominator beyond 1 whole</li></ul>
Year 5	<ul style="list-style-type: none"><li>• Add using mental strategies</li><li>• Add whole numbers with more than 4 digits</li><li>• Add decimals with up to 2 decimal places</li><li>• Complements to 1</li><li>• Add fractions with denominators that are a multiple of one another</li></ul>
Year 6	<ul style="list-style-type: none"><li>• Add integers up to 10 million</li><li>• Add decimals with up to 3 decimal places</li><li>• Order of operations</li><li>• Negative numbers</li><li>• Add fractions</li></ul>



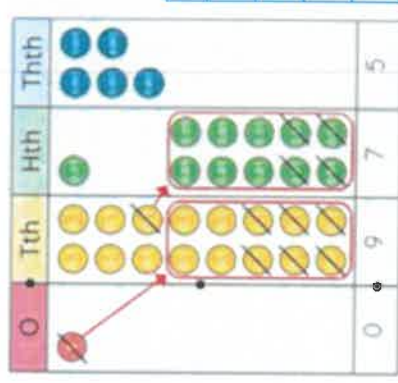
# Addition

Progression of skills	Key representations	
<p><b>Order of operations</b></p> <p>Calculations in brackets should be done first. Multiplication and division should be performed before addition and subtraction. *When no brackets are shown and the operations have the <b>same</b> priority, work left to right.</p>	<p>... has greater priority than ..., so the first part of the calculation I need to do is ...</p>   <p><math>(3 + 4) \times 2 = 14</math></p>  <p><math>3 \times 4 + 2 = 14</math></p>  <p><math>3 + 4 \times 2 = 11</math></p>	
<p><b>Negative numbers</b></p> <p>Children add to negative numbers and carry out calculations which cross 0</p>	<p>... plus ... is equal to ...</p>  <p><math>-3 + 5 = 2</math></p>  <p><math>-11 + 16 = 5</math></p>  <p>The difference between <math>-5</math> and <math>-1</math> is <math>4</math></p>  <p>The difference between <math>-5</math> and <math>5</math> is <math>10</math></p>	

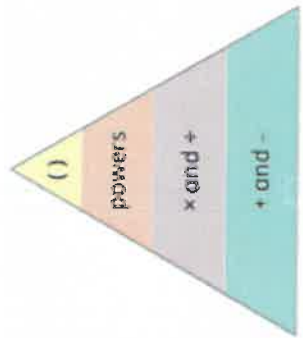
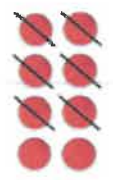
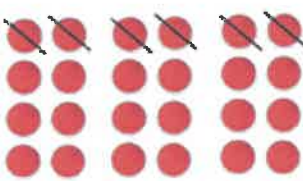

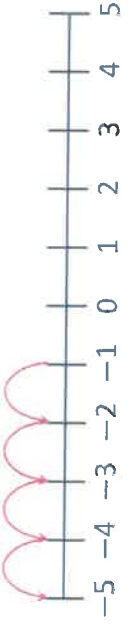
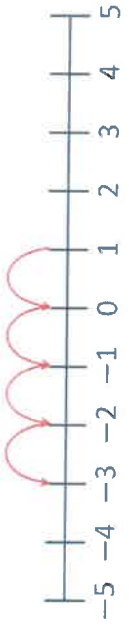
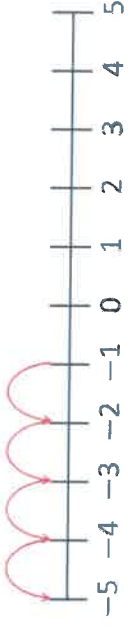
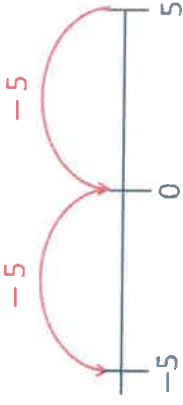
# Addition

Progression of skills	Key representations		
<p><b>Add fractions</b></p> <p>Convert fractions to the same denominator before adding. Progress from fractions where one denominator is a multiple of the other, to any fractions and then to mixed numbers.</p>	<p>The denominator has been multiplied by ..., so the numerator needs to be multiplied by ...</p> 	<p>The lowest common multiple of ... and ... is ...</p>  $\frac{1}{3} + \frac{1}{4} = \frac{4}{12} + \frac{3}{12} = \frac{7}{12}$	<p>...is made up of ... wholes and ...</p> 

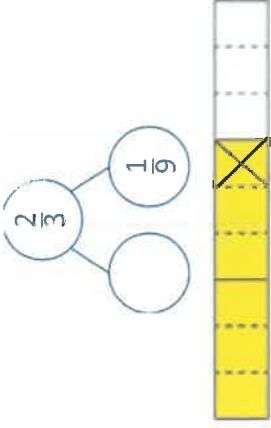
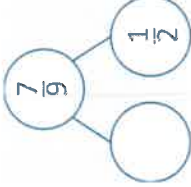
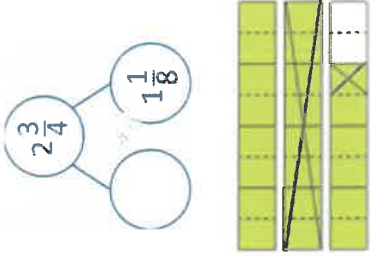
# Subtraction

<p>Year 6</p>	<ul style="list-style-type: none"> <li>Subtract larger numbers, using the formal written methods of columnar subtraction.</li> <li>Use their knowledge of the order of operations to carry out calculations involving the 4 operations.</li> <li>Calculate intervals across zero.</li> <li>Subtract fractions with different denominators and mixed numbers, using the concept of equivalent fractions.</li> </ul>																																					
<p><b>Key representations</b></p>																																						
<p><b>Subtract integers up to 10 million</b></p> <p>Encourage children to estimate and use inverse operations to check answers to calculations.</p>	<table border="1" style="margin-bottom: 10px;"> <tr><td>2</td><td>1</td><td>4</td><td>5</td><td>1</td><td>2</td><td>1</td></tr> <tr><td>-</td><td>1</td><td>8</td><td>4</td><td>3</td><td>2</td><td>1</td></tr> <tr><td></td><td>1</td><td>6</td><td>1</td><td>9</td><td>0</td><td>0</td></tr> </table> <table border="1" style="margin-bottom: 10px;"> <tr><td>4,604</td></tr> <tr><td>2,354</td></tr> <tr><td>750</td></tr> <tr><td>?</td></tr> </table> <table border="1" style="margin-bottom: 10px;"> <tr><td>8</td><td>4</td><td>8</td><td>5</td></tr> <tr><td>-</td><td>3</td><td>6</td><td>4</td></tr> <tr><td></td><td>5</td><td>5</td><td>5</td></tr> </table>	2	1	4	5	1	2	1	-	1	8	4	3	2	1		1	6	1	9	0	0	4,604	2,354	750	?	8	4	8	5	-	3	6	4		5	5	5
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<p><b>Subtract decimals with up to 3 decimal places</b></p> <p>Progress from the same number of decimal and whole number places to a different number of decimal and whole number places.</p>	<p>I do/do not need to make an exchange because ...</p> <table border="1" style="margin-bottom: 10px;"> <tr><td>6</td><td>7</td><td>1</td><td>3</td></tr> <tr><td>-</td><td>1</td><td>3</td><td>4</td></tr> <tr><td></td><td>5</td><td>3</td><td>9</td></tr> </table>  <table border="1" style="margin-bottom: 10px;"> <tr><td>0</td><td>9</td><td>7</td><td>5</td></tr> <tr><td>-</td><td>0</td><td>6</td><td>4</td></tr> <tr><td></td><td>0</td><td>9</td><td>7</td></tr> </table> <table border="1" style="margin-bottom: 10px;"> <tr><td>0</td><td>5</td><td>1</td><td>5</td></tr> <tr><td>-</td><td>0</td><td>6</td><td>4</td></tr> <tr><td></td><td>0</td><td>9</td><td>7</td></tr> </table>	6	7	1	3	-	1	3	4		5	3	9	0	9	7	5	-	0	6	4		0	9	7	0	5	1	5	-	0	6	4		0	9	7	
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# Subtraction

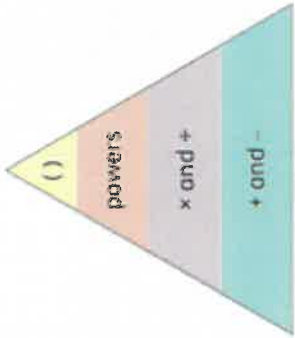
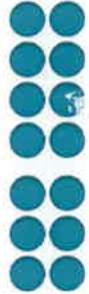




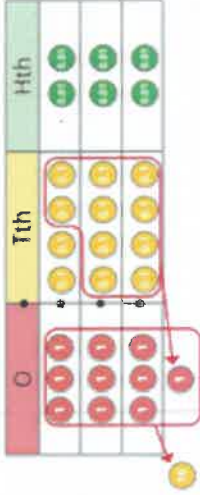
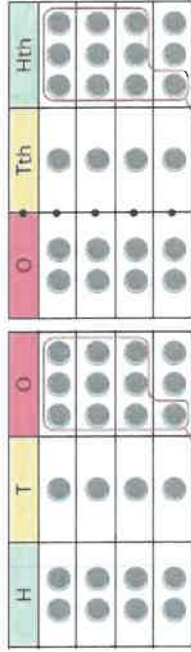

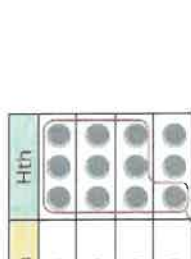
Progression of skills	Key representations	
<p><b>Order of operations</b></p> <p>Children learn the order of priority for operations in a calculation. Calculations in brackets should be done first. Multiplication and division should be performed before addition and subtraction.</p>	<p>... has greater priority than ..., so the first part of the calculation I need to do is ...</p>   $8 - 2 \times 3 = 2$  $(8 - 2) \times 3 = 18$  $8 - 2^2 = 4$	<p><b>Negative numbers</b></p> <p>Children subtract from positive and negative numbers and calculate intervals across 0</p> <p>... minus ... is equal to ...</p>  $-1 - 4 = -5$  $1 - 4 = -3$
	 <p>The difference between -5 and -1 is 4</p>  <p>The difference between 5 and -5 is 10</p>	

# Subtraction

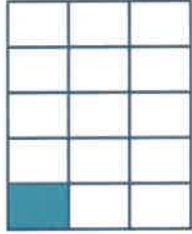
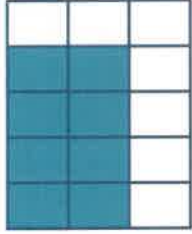
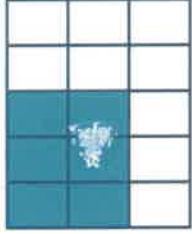
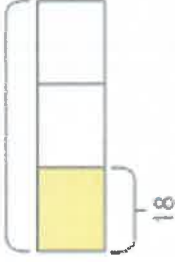
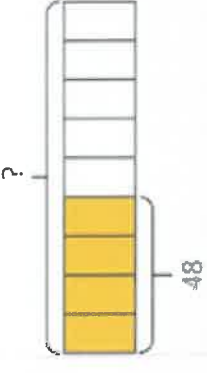
Progression of skills	Key representations		
<p><b>Subtract fractions</b></p> <p>Convert fractions to the same denominator before subtracting. Progress from fractions where one denominator is a multiple of the other, to any fractions and then subtracting from a mixed number.</p>	<p>The denominator has been multiplied by ..., so the numerator needs to be multiplied by...</p>  $\frac{2}{3} - \frac{1}{9} = \frac{6}{9} - \frac{1}{9} = \frac{5}{9}$	<p>The lowest common multiple of ... and ... is ...</p>  $\frac{7}{9} - \frac{1}{2} = \frac{14}{18} - \frac{9}{18} = \frac{5}{18}$	<p>... is made up of ... wholes and ...</p>  $2\frac{3}{4} - 1\frac{1}{8} = 1\frac{5}{8}$



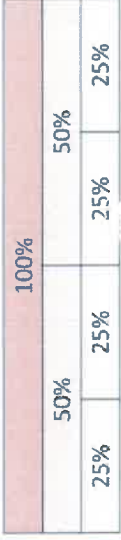


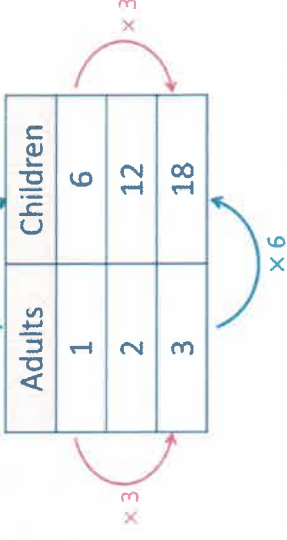
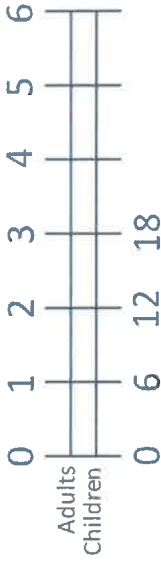
# Multiplication

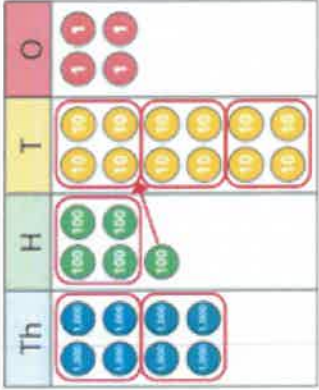
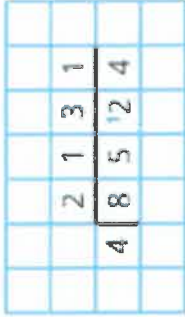
Progression of skills	Key representations
<p><b>Order of operations</b></p> <p>Calculations in brackets should be done first. Multiplication and division should be performed before addition and subtraction.</p>	<p>... has greater priority than ..., so the first part of the calculation I need to do is ...</p>  <div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;">  <p><math>(3 + 4) \times 2 = 14</math></p> </div> <div style="text-align: center;">  <p><math>3 + 4^2 = 19</math></p> </div> <div style="text-align: center;">  <p><math>3 + 4 \times 2 = 11</math></p> </div> </div>
<p><b>Multiply decimals by integers</b></p> <p>This is the first time children multiply decimals by numbers other than 10, 100 or 1,000. Encourage them to make links with known facts and whole number multiplication.</p>	<p>I know that <math>... \times ... = ...</math>, so I also know that <math>... \times ... = ...</math></p> <div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;">  <p><math>6 \times 2 = 12</math></p> </div> <div style="text-align: center;">  <p><math>6 \times 0.2 = 1.2</math></p> </div> </div> <p>I need to exchange 10 ... for 1 ...</p> <div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;">  </div> <div style="text-align: center;">  </div> </div> <div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;">  </div> <div style="text-align: center;">  </div> </div> <div style="display: flex; justify-content: space-around; align-items: center; margin-top: 20px;"> <div style="text-align: center;"> <p><math>213 \times 4 = 852</math></p> </div> <div style="text-align: center;"> <p><math>2.13 \times 4 = 8.52</math></p> </div> </div>

# Multiplication

Progression of skills	Key representations	
<p>Multiply fractions by fractions</p> <p>Encourage children to give answers in their simplest form.</p>	<p>When multiplying a pair of fractions, I need to multiply the numerator and multiply the denominator.</p> <div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;">  <p><math>\frac{1}{3} \times \frac{1}{5} = \frac{1}{15}</math></p> </div> <div style="text-align: center;">  <p><math>\frac{2}{3} \times \frac{4}{5} = \frac{8}{15}</math></p> </div> <div style="text-align: center;">  <p><math>\frac{2}{3} \times \frac{2}{5} = \frac{4}{15}</math></p> </div> </div>	
<p><b>Find the whole</b></p> <p>Children multiply to find the whole from a given part.</p>	<p>If <math>\frac{1}{\square}</math> is ..., then the whole is ... X ...</p> <p><math>\frac{1}{3}</math> of <math>\square = 18</math></p>  <p><math>18 \times 3 = 54</math></p> <p><math>\frac{1}{3}</math> of <b>54</b> = 18</p>	<p>If <math>\frac{\square}{\square}</math> is ..., then <math>\frac{1}{\square}</math> is ... and the whole is ... X ...</p> <p><math>\frac{4}{9}</math> of <math>\square = 48</math></p>  <p><math>\frac{1}{9} = 48 \div 4 = 12</math></p> <p><math>9 \times 12 = 108</math></p> <p><math>\frac{4}{9}</math> of <b>108</b> = 48</p>

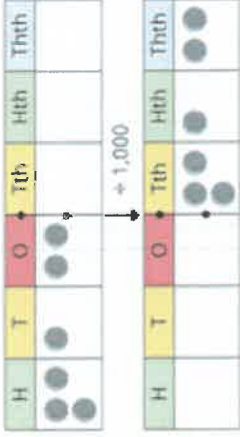

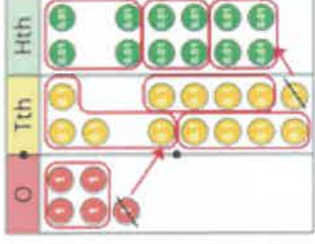

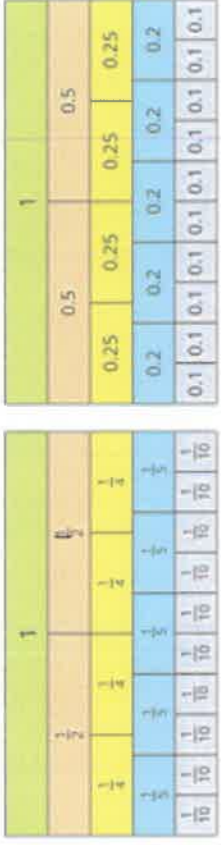

# Multiplication

Progression of skills	Key representations																													
<p><b>Calculate percentages</b></p> <p>Children first learn how to find 1%, 10%, 20%, 25% and 50% before using multiples of these amounts to find any percentage.</p>	<p>There are ... lots of ... % in 100%</p> <p>To find ... %, I need to divide by ...</p>  <table border="1" data-bbox="427 1043 547 1581"> <tr> <td colspan="2">100%</td> </tr> <tr> <td>50%</td> <td>50%</td> </tr> <tr> <td>25%</td> <td>25%</td> </tr> <tr> <td>25%</td> <td>25%</td> </tr> </table> <p>50% of ... = ... ÷ 2</p> <p>25% of ... = ... ÷ 4</p>	100%		50%	50%	25%	25%	25%	25%	<p>... % is made up of ... %, and ... %</p>  <table border="1" data-bbox="411 185 507 981"> <tr> <td colspan="10">100%</td> </tr> <tr> <td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td> </tr> </table> <p>To find 30%, I can find 10% and then multiply it by 3</p> <p>To find 23%, I can use 10% × 2 and 1% × 3</p> <p>To find 99%, I can find 1%, then subtract from 100%</p>	100%										10%	10%	10%	10%	10%	10%	10%	10%	10%	10%
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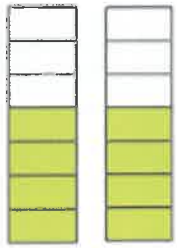
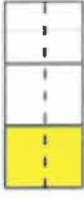
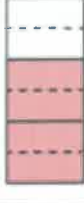
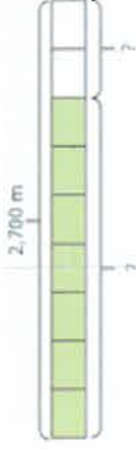
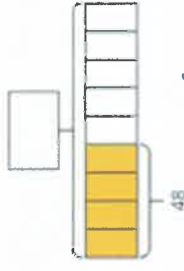
<p><b>Year 6</b></p>	<ul style="list-style-type: none"> <li>• Perform mental calculations, including with mixed operations and large numbers.</li> <li>• Divide numbers up to 4 digits by a two-digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context.</li> <li>• Divide numbers up to 4 digits by a two-digit number using the formal written method of short division where appropriate, interpreting remainders according to the context.</li> <li>• Divide numbers by 10, 100 and 1,000 giving answers up to three decimal places.</li> <li>• Use written division methods in cases where the answer has up to two decimal places.</li> <li>• Associate a fraction with division and calculate decimal fraction equivalents.</li> <li>• Divide proper fractions by whole numbers [for example, <math>\frac{1}{3} \div 2 = \frac{1}{6}</math> ]</li> <li>• Solve problems involving the calculation of percentages.</li> </ul>
<p><b>Progression of skills</b></p>	<p><b>Key representations</b></p>
<p><b>Short division</b></p> <p>Encourage children to interpret remainders in context, for example knowing that “4 remainder 1” could mean 4 complete boxes with 1 left over so 5 boxes will be needed.</p>	<p>There are ... groups of ... hundreds/tens/ones/ in ... I can exchange 1 ... for 10 ...</p>  

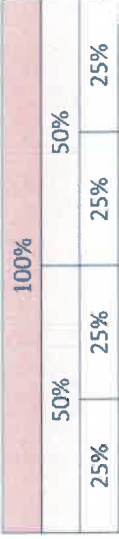



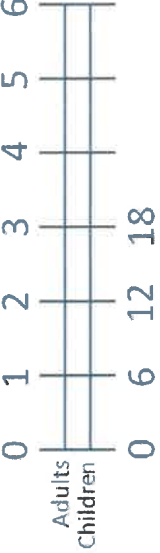
# Division

Progression of skills		Key representations	
<b>Mental strategies</b>	<p>To divide by ..., I can first divide by ... and then divide the answer by ...</p> <p>240 ÷ 60 = 240 ÷ 10 ÷ 6</p> <p>240 → ÷ 10 → [ ] → ÷ 6 → [ ]</p> <p>480 ÷ 24 = 480 ÷ 4 ÷ 6</p> <p>480 → ÷ 4 → [ ] → ÷ 6 → [ ]</p> <p>9,120 ÷ 15 = 9,120 ÷ 5 ÷ 3</p>		
<b>Long division</b>	<p>The long division method is introduced for the first time. Two alternative methods are shown.</p>	<p><b>Method 1</b></p>	<p><b>Method 2</b></p>
<b>Order of operations</b>	<p>Calculations in brackets should be done first, then powers. Multiplication and division should be performed before addition and subtraction.</p>	<p>... has greater priority than ..., so the first part of the calculation I need to do is ...</p> <p>(6 + 4) ÷ 2 = 5</p> <p>6 + 4 ÷ 2 = 8</p>	

Progression of skills	Key representations	
<p><b>Divide by 10, 100 and 1,000</b></p> <p>Encourage children to notice that dividing by 100 is the same as dividing by 10 twice, and that dividing by 1,000 is the same as dividing by 10 three times.</p>	<p>To divide by ..., I move the digits ... places to the right.</p>  <p> <math>312 \div 10 = 31.2</math>  <math>312 \div 100 = 3.12</math>  <math>312 \div 1,000 = 0.312</math> </p>	<p> <math>906 \div 10 = 90.6</math>  <math>906 \div 100 = 9.06</math>  <math>906 \div 1,000 = 0.906</math> </p>
<p><b>Divide decimals by integers</b></p> <p>This is the first time children divide decimals by numbers other than 10, 100 or 1,000</p>	<p>I know that ... <math>\div</math> ... = ..., so I also know that ... <math>\div</math> ... = ...</p>  <p> <math>39 \div 3 = 13</math>     <math>3.9 \div 3 = 1.3</math>     <math>0.39 \div 3 = 0.13</math> </p>	<p>I need to exchange 1 ... for 10 ...</p>  
<p><b>Decimal and fraction equivalents</b></p>	<p>The fraction ... is equivalent to the decimal ...</p>  <p> <math>\frac{1}{5} = 0.2</math>     <math>\frac{2}{5} = 0.4</math>     <math>\frac{3}{5} = 0.6</math> </p>  <p> <math>\frac{3}{4}</math> is equal to <math>\frac{75}{100}</math> </p>  <p> <math>\frac{3}{4} = \frac{75}{100} = 0.75</math> </p>	

# Division

Progression of skills	Key representations		
<p><b>Divide a fraction by an integer</b></p> <p>This is the first time children divide fractions by an integer.</p>	<p>... ones divided by 2 is ... ones so ... sevenths divided by 2 is ... sevenths.</p>  $\frac{4}{7} \div 2 = \frac{2}{7}$ $\frac{4}{7} \div 2 = \frac{2}{7}$	<p>I am dividing by ..., so I can split each part into ... equal parts.</p>  $\frac{1}{3} \div 2 = \frac{1}{6}$	<p>... is equivalent to ... so ... <math>\div</math> ... = ... <math>\div</math> ...</p>  $\frac{2}{3} \div 4 = \frac{4}{6} = 1 \frac{1}{6}$
<p><b>Fraction of an amount</b></p> <p>Children divide and multiply to find fractions of an amount. Bar models can still be used to support understanding where needed.</p>	<p>To find <math>\frac{1}{2}</math> I divide by ...</p> $\frac{1}{2} \text{ of } 36 = 36 \div 2$ $\frac{1}{12} \text{ of } 36 = 36 \div 12$	<p>If <math>\frac{1}{9}</math> is equal to ..., then <math>\frac{7}{9}</math> are equal to ...</p>  $\frac{7}{9} \text{ of } 2,700 = \frac{1}{9} \text{ of } 2,700 \times 7$	<p>If <math>\frac{4}{9}</math> is equal to ..., then the whole is equal to ...</p>  $\frac{4}{9} \text{ of } \underline{\quad} = 48$

Progression of skills	Key representations									
<p><b>Calculate percentages</b></p> <p>Children first learn how to find 1%, 10%, 20%, 25% and 50% before using multiples of these amounts to find any percentage.</p>	<p>There are ... lots of ... % in 100%</p> <p>To find ... %, I need to divide by ...</p>  <p>50% of ... = ... ÷ 2</p> <p>25% of ... = ... ÷ 4</p>	<p>... % is made up of ... %, and ... %</p>  <p>To find 30%, I can find 10% and then multiply it by 3</p> <p>To find 23%, I can use 10% × 2 and 1% × 3</p> <p>To find 99%, I can find 1%, then subtract from 100%</p>								
<p><b>Calculations involving ratio</b></p> <p>Encourage children to see the multiplicative relationship between ratios. They will need to multiply or divide each value by the same number to keep the ratio equivalent. Double number lines and ratio tables help children to see both horizontal and vertical multiplicative relationships.</p>	<p>For every ... , there are ...</p> <p>For every 6 children on a school trip, there is 1 adult.</p> <div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;">  <p>adults</p> </div> <div style="text-align: center;">  <p>children</p> </div> </div> <p>The ratio of children to adults is 6 : 1</p> <div style="display: flex; justify-content: space-around; align-items: center; margin-top: 20px;"> <table border="1" data-bbox="842 161 1050 600"> <thead> <tr> <th>Adults</th> <th>Children</th> </tr> </thead> <tbody> <tr> <td>1</td> <td>6</td> </tr> <tr> <td>2</td> <td>12</td> </tr> <tr> <td>3</td> <td>18</td> </tr> </tbody> </table> <div style="margin-left: 20px;">  </div> </div>		Adults	Children	1	6	2	12	3	18
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